

## Key Stage 3 Medium-term plans

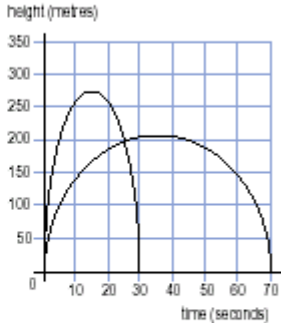
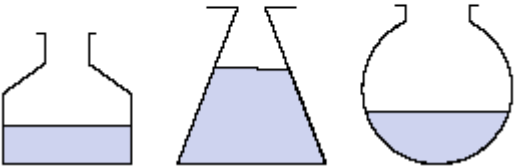
**Year 9: Core (Pupils that have achieved levels 5c – 5a)****Autumn term****Teaching objectives for the oral and mental activities**

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| <ul style="list-style-type: none"><li>• Order, add, subtract, multiply and divide integers.</li><li>• Multiply and divide decimals by 10, 100, 1000, 0.1 and 0.01.</li><li>• Count on and back in steps of 0.4, 0.75, <math>\frac{3}{4}</math>...</li><li>• Round numbers, including to one or two decimal places.</li><li>• Know and use squares, cubes, roots and index notation.</li><li>• Know or derive quickly prime numbers less than 30 and factor pairs for a given number.</li><li>• Convert between fractions, decimals and percentages.<br/>Know that 0.005 is half of one per cent.</li><li>• Find fractions and percentages of quantities.</li><br/><li>• Know or derive complements of 0.1, 1, 10, 50, 100, 1000.</li><li>• Add and subtract several small numbers or several multiples of 10, e.g. <math>250 + 120 - 190</math>.</li><li>• Use jottings to support addition and subtraction of whole numbers and decimals.</li><li>• Use knowledge of place value to multiply and divide, e.g. <math>432 \times 0.01</math>, <math>37 \div 0.01</math>, <math>0.04 \times 8</math>, <math>0.03 \div 5</math>, <math>13 \times 1.4</math>.</li><li>• Recall multiplication and division facts to <math>10 \times 10</math>. Derive products and quotients of multiples of 10, 100, 1000.</li><li>• Use factors to multiply and divide mentally, e.g. <math>22 \times 0.02</math>, <math>420 \div 15</math>.</li></ul> | <ul style="list-style-type: none"><li>• Multiply and divide a two-digit number by a one-digit number.</li><li>• Use approximations to estimate the answers to calculations, e.g. <math>39 \times 2.8</math>.</li><br/><li>• Solve equations, e.g. <math>n(n - 1) = 56</math>, <math>\square + \square = 46</math>.</li><br/><li>• Visualise, describe and sketch 2-D shapes.</li><li>• Recall and use formulae for the perimeter of a rectangle, and areas of rectangles and triangles.</li><li>• Calculate volumes of cuboids.</li><li>• Estimate and order acute, obtuse and reflex angles.</li><br/><li>• Use metric units (length, mass, capacity) and units of time for calculations.</li><li>• Use metric units for estimation (length, mass, capacity).</li><li>• Convert between metric units, including area, volume and capacity measures.</li><br/><li>• Discuss and interpret graphs.</li><li>• Calculate a mean using an assumed mean.</li><br/><li>• Apply mental skills to solve simple problems.</li></ul> |
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## Algebra 1/2 (2 weeks)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources						
<p><b>Sequences, functions and graphs (148–163, 172–177)</b></p> <p><b>Generate terms of a sequence using term-to-term and position-to-term definitions of the sequence, on paper and using ICT. 5a – 6c</b></p> <p>Generate sequences from practical contexts and <b>write an expression to describe the <math>n</math>th term of an arithmetic sequence. 6c</b></p> <p><b>Find the inverse of a linear function. 5b</b></p>	<p><b>Generate a sequence given a rule for finding each term from its position in the sequence</b>, referring to terms as <math>T(1)</math> = first term, <math>T(2)</math> = second term, ..., <math>T(n)</math> = <math>n</math>th term. For example:</p> <ul style="list-style-type: none"> <li>The <math>n</math>th term of a sequence is <math>2n</math>, i.e. <math>T(n) = 2n</math>. Write the first five terms.</li> <li>Write the first five terms of a sequence whose <math>n</math>th term or <math>T(n)</math> is:           <table style="margin-left: 20px; border: none;"> <tr> <td>a. <math>5n + 4</math></td> <td>c. <math>99 - 9n</math></td> <td>e. <math>3n - 0.1</math></td> </tr> <tr> <td>b. <math>105 - 5n</math></td> <td>d. <math>n + \frac{1}{2}</math></td> <td>f. <math>n \times 0.1</math></td> </tr> </table> </li> </ul> <p>Find the <math>n</math>th term of any linear (arithmetic) sequence. For example:</p> <ul style="list-style-type: none"> <li>Find the <math>n</math>th term of 21, 27, 33, 39, 45, ...</li> </ul> <p>The difference between successive terms is 6, so the <math>n</math>th term is of the form <math>T(n) = 6n + b</math>.  <math>T(1) = 21</math>, so <math>6 + b = 21</math>, leading to <math>b = 15</math>.  <math>T(n) = 6n + 15</math>            Check by testing a few terms. <li>Find the <math>n</math>th term of these sequences:            54, 62, 70, 78, 86, ...            68, 61, 54, 47, 40, ...            2.3, 2.5, 2.7, 2.9, 3.1, ...            -5, -14, -23, -32, -41, ...</li> </p>	a. $5n + 4$	c. $99 - 9n$	e. $3n - 0.1$	b. $105 - 5n$	d. $n + \frac{1}{2}$	f. $n \times 0.1$	
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## Algebra 1/2 (continued)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources
<p><b>Construct functions arising from real-life problems and plot their corresponding graphs. 6a</b></p>	<p>Draw and use graphs to solve distance–time problems. For example:</p> <ul style="list-style-type: none"> <li>This graph shows how high two rockets went during a flight. Rocket A reached a greater height than rocket B.</li> </ul>  <p>Estimate how much higher rocket A reached than rocket B.</p> <p>Estimate the time after the start when the two rockets were at the same height.</p> <p>Estimate the number of seconds that rocket A was more than 200 m above the ground.</p> <p>Sketch a graph of the depth of water against time when water drips steadily from a tap into these bottles.</p> 	<p>9.3 chapter 14  <a href="#">LINK TO SCIENCE GEOGRAPHY</a></p>

## Algebra 1/2 (continued)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources
<p><b>Solving problems (26–27)</b></p> <p><b>Represent problems and synthesise information in algebraic, geometric or graphical form; move from one form to another to gain a different perspective on the problem. 5b – 6b</b></p>	<p><i>Five coins</i></p> <p>A game involves tossing five coins for a 10p stake. If you score exactly two heads you win 20p and get your stake back; otherwise you lose. Give mathematical reasons to justify whether this is a sensible game to play.</p> <p>Related objectives: Present a proof, making use of symbols, diagrams and graphs and related explanatory text; <i>justify generalisations and choice of presentation, explaining selected features.</i></p>	<p><b>GAMBLING PREDICTIONS</b></p>

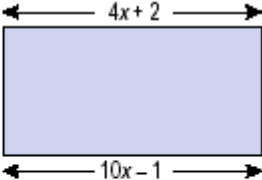
## Number 1 (3 weeks)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources
<p><b>Proportional reasoning, including: Fractions, decimals, percentages, ratio and proportion (66–81)</b></p> <ul style="list-style-type: none"><li>• <b>Use efficient methods to add, subtract, multiply and divide fractions, interpreting division as a multiplicative inverse; cancel common factors before multiplying or dividing. 5a – 6a</b></li><li>• <b>Recognise when fractions or percentages are needed to compare proportions; solve problems involving percentage changes. 6a</b></li><li>• <b>Use proportional reasoning to solve a problem, choosing the correct numbers to take as 100%, or as a whole; compare two ratios; interpret and use ratio in a range of contexts, including solving word problems. 5a – 6b</b></li></ul>	<ul style="list-style-type: none"><li>• A slogan on a tube of mints says that it is 23% bigger. It contains 20 mints. How many mints are there in the normal tube?</li><li>• Which is the better buy: a 400 g pack of biscuits at 52p, or a pack of biscuits with 400 g + 25% extra, at 57p?</li><li>• In a phone bill, VAT at 17.5% is added to the total cost of calls and line rental. What percentage of the total bill is VAT?</li><li>• In 1999, about 50% of the world's tropical rain forests had been destroyed. About 180 000 square kilometres are now destroyed each year. This represents about 1.2% of the remainder. Estimate the original area of the tropical rain forests.</li></ul>	<p><b>SCIENCE GEOGRAPHY FINANCE BUSINESS STUDIES</b></p>

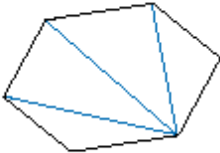
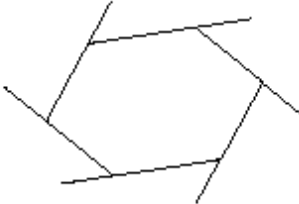
## Number 1 (continued)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources
<p><b>Calculations (82–103, 110–111)</b></p> <p><b>Understand the effects of multiplying and dividing by numbers between 0 and 1; use the laws of arithmetic and inverse operations. 5a – 6c</b></p> <p><b>Use known facts to derive unknown facts; extend mental methods of calculation, working with decimals, fractions, percentages, factors, powers and roots; solve word problems mentally. 5a – 6b</b></p> <p><b>Make and justify estimates and approximations of calculations. 5c – 6b</b></p>	<p>Apply mental skills to solving simple problems, using jottings if appropriate. For example:</p> <p><b>Oral questions</b></p> <ul style="list-style-type: none"> <li>Two years ago Jim’s height was 1.48 metres. Now Jim’s height is 1.7 metres. How much has Jim grown?</li> <li>Two of the angles of a triangle are <math>47^\circ</math> and <math>85^\circ</math>. Calculate the third angle.</li> <li>You get \$56 for £40. How many dollars do you get for £100?</li> <li>75 miles per hour is about the same as 33 metres per second. About how many metres per second is 50 miles per hour?</li> <li>In a raffle, half of the tickets are bought by men. One third are bought by women. The rest are bought by children. What fraction of the tickets are bought by children?</li> <li>The ratio of men to women in a room is 3 to 5. There are 12 men. How many women are there?</li> <li><math>x = 2</math> and <math>y = 3</math>. Work out the value of <math>x</math> to the power <math>y</math> plus <math>y</math> to the power <math>x</math>.</li> </ul> <p>Make and justify estimates of calculations such as:</p> <ul style="list-style-type: none"> <li><math>(2095 \times 302) + 396</math></li> <li><math>3.75 \times (2.36 - 0.39)</math></li> <li><math>\frac{103 \times 0.44}{\sqrt{16.1}}</math></li> </ul>	<p><b>NUMERACY</b></p>

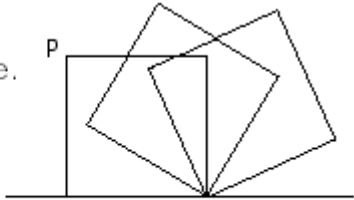
### Algebra 3 (2 weeks)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources								
<p><b>Equations, formulae and identities (112–113, 122–125, 132–137)</b></p> <ul style="list-style-type: none"> <li>Distinguish the different roles played by letter symbols in equations, identities, formulae and functions. <b>5c – 6b</b></li> <li>Construct and solve linear equations with integer coefficients (with and without brackets, negative signs anywhere in the equation, positive or negative solution) using an appropriate method. <b>6c – 6a</b></li> <li>Use systematic trial and improvement methods and ICT tools to find approximate solutions of equations such as <math>x^3 + x = 20</math>. <b>6b - 6a</b></li> <li>Solve problems involving direct proportion using algebraic methods, relating algebraic solutions to graphical representations of the equations; use ICT as appropriate. <b>6c – 6a</b></li> </ul>	<p>The length of a rectangle is three times its width. Its perimeter is 24 centimetres. Find its area.</p> <p>The area of this rectangle is <math>10 \text{ cm}^2</math>.</p>  <p>Calculate the value of <math>x</math> and use it to find the length and width of the rectangle.</p> <p>The length of one side of a rectangle is <math>y</math>. This equation shows the area of the rectangle.</p> $y(y + 2) = 67.89$ <p>Find the value of <math>y</math>. Show your working.</p> <p>You may find this table helpful.</p> <table border="1" data-bbox="1010 1117 1375 1281"> <thead> <tr> <th><math>y</math></th> <th><math>y + 2</math></th> <th><math>y(y + 2)</math></th> <th></th> </tr> </thead> <tbody> <tr> <td>8</td> <td>10</td> <td>80</td> <td>too large</td> </tr> </tbody> </table>	$y$	$y + 2$	$y(y + 2)$		8	10	80	too large	<p><b>D&amp;T</b> <b>CONSTRUCTION INDUSTRY</b> <b>SCIENCE</b></p>
$y$	$y + 2$	$y(y + 2)$								
8	10	80	too large							

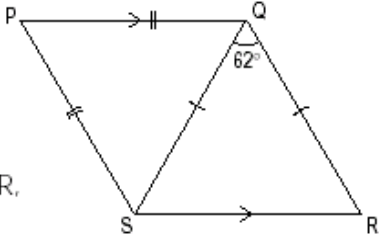
## Shape, space and measures 1 (3 weeks)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources
<p><b>Geometrical reasoning: lines, angles and shapes (178–189, 194–197)</b></p> <ul style="list-style-type: none"> <li>• Distinguish between conventions, definitions and derived properties. <b>6c</b></li> <li>• Explain how to find, calculate and use: <ul style="list-style-type: none"> <li>- the sums of the interior and exterior angles of quadrilaterals, pentagons and hexagons, <b>6b</b></li> <li>- the interior and exterior angles of regular polygons. <b>6b</b></li> </ul> </li> <li>• Solve problems using properties of angles, of parallel and intersecting lines, and of triangles and other polygons, justifying inferences and explaining reasoning with diagrams and text. <b>5a – 6a</b></li> <li>• Know the definition of a circle and the names of its parts; explain why inscribed regular polygons can be constructed by equal divisions of a circle. <b>6b – 6a</b></li> </ul>	<p>Explain how to find the interior angle sum and the exterior angle sum in (irregular) quadrilaterals, pentagons and hexagons. For example:</p> <ul style="list-style-type: none"> <li>• A polygon with <math>n</math> sides can be split into <math>n - 2</math> triangles, each with an angle sum of <math>180^\circ</math>.</li> </ul>  <p>So the interior angle sum is <math>(n - 2) \times 180^\circ</math>, giving <math>360^\circ</math> for a quadrilateral, <math>540^\circ</math> for a pentagon and <math>720^\circ</math> for a hexagon.</p> <p>At each vertex, the sum of the interior and exterior angles is <math>180^\circ</math>.</p>  <p>For <math>n</math> vertices, the sum of <math>n</math> interior and <math>n</math> exterior angles is <math>n \times 180^\circ</math>. But the sum of the interior angles is <math>(n - 2) \times 180^\circ</math>, so the sum of the exterior angles is always <math>2 \times 180^\circ = 360^\circ</math>.</p>	

## Shape, space and measures 1 (continued)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources
<p><b>Construction and loci (220–227)</b></p> <p><b>Use straight edge and compasses to construct a triangle, given right angle, hypotenuse and side (RHS); use ICT to explore constructions of triangles and other 2-D shapes. 6a</b></p> <p><b>Find the locus of a point that moves according to a simple rule, both by reasoning and by using ICT. 7a</b></p>	<p>Use the method for constructing a perpendicular from a point on a line to construct triangles, given right angle, hypotenuse and side (RHS). For example:</p> <ul style="list-style-type: none"> <li>• A 10 metre ladder rests against a wall with its foot 3 metres away from the wall. Construct a diagram to scale. Then use a ruler and protractor to measure as accurately as possible:             <ol style="list-style-type: none"> <li>a. how far up the wall the ladder reaches;</li> <li>b. the angle between the ladder and the ground.</li> </ol> </li> </ul> <p>Imagine a square being rolled along a straight line. What path would the point P trace?</p>  <p>A spider is dangling motionless on a single web. I move a finger so that its tip is always 10 cm from the spider. What is the locus of my fingertip? <i>(The surface of a sphere.)</i></p> <p>I hold a ruler in my left hand, then move the tip of my right forefinger so that it is always 8 cm from the ruler. What is the locus of my fingertip? <i>(The surface of a cylinder with a hemisphere on each end.)</i></p>	

## Shape, space and measures 1 (continued)

Learning objectives – what should the pupils be able to do?	Outcomes – what will success look like?	Resources
<p><b>Solving problems (14–17)</b></p> <p><b>Explore connections in mathematics across a range of contexts: shape and space. 5a – 6a</b></p>	<p>For example:</p>  <ul style="list-style-type: none"> <li>In the diagram:  <math>PQ = PS</math>,  <math>QR = QS</math>,  <math>PQ</math> is parallel to <math>SR</math>,                      angle <math>SQR</math> is <math>62^\circ</math>.                      Calculate the sizes of the other angles.</li> </ul> <p>Triangle <math>T</math> has vertices at <math>(1, 2)</math>, <math>(2, 4)</math> and <math>(3, 4)</math>.</p> <ol style="list-style-type: none"> <li>Draw <math>T</math> on squared paper.</li> <li>Triangle <math>R</math> is obtained by reflecting <math>T</math> in the <math>x</math>-axis. Draw <math>R</math>. What are the coordinates of its vertices?</li> <li>Triangle <math>S</math> is obtained by reflecting <math>R</math> in the <math>y</math>-axis. Draw <math>S</math>. What are its coordinates?</li> <li>There is a transformation that takes triangle <math>T</math> directly to triangle <math>S</math>. Describe this transformation as precisely as you can.</li> </ol>	